

83. Pentaquarks

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Experimental searches for pentaquark hadrons comprised of light flavors have a long and vivid history. No undisputed candidates had been found in 50 years. The first wave of claimed observations of pentaquark candidates containing a strange antiquark occurred in the early seventies, see e.g. a review in the 1976 edition of Particle Data Group listings for $Z_0(1780)$, $Z_0(1865)$ and $Z_1(1900)$ [1]. The last mention of these candidates can be found in the 1992 edition [2] with the perhaps prophetic comment “the results permit no definite conclusion - the same story for 20 years. [...] The skepticism about baryons not made of three quarks, and lack of any experimental activity in this area, make it likely that another 20 years will pass before the issue is decided.” A decade later, a second wave of observations occurred, possibly motivated by specific theoretical predictions for their existence [3–5]. The evidence for pentaquarks was based on observations of peaks in the invariant mass distributions of their decay products. More data and subsequent more sensitive experiments did not confirm these claims [6]. In the last mention of the best known candidate from that period, $\Theta(1540)^+$, the 2006 Particle Data Group listing [7] included a statement: “The conclusion that pentaquarks in general, and that Θ^+ , in particular, do not exist, appears compelling.” which well reflected the prevailing mood in the particle physics community until a study of $\Lambda_b^0 \rightarrow J/\psi p K^-$ ($J/\psi \rightarrow \mu^+ \mu^-$) decays by LHCb [8] (charge conjugate modes are implied). From an analysis of 3 fb^{-1} Run 1 data at 7 and 8 TeV at the LHC, the LHCb collaboration reported a significant $J/\psi p$ structure in $\Lambda_b^0 \rightarrow J/\psi p K^-$ decays [8]. The exotic character of this structure, with the minimal quark content of $uudc\bar{c}$, was demonstrated in a nearly model-independent way in Ref. [9], where it was shown that the $J/\psi p$ mass ($m_{J/\psi p}$) peak near 4450 MeV was too narrow to be accounted for by $\Lambda^* \rightarrow p K^-$ reflections (Λ^* denotes a generic Λ excitation), reinforcing the results from the earlier model-dependent six-dimensional amplitude analysis of invariant masses and decay angles describing the Λ_b^0 decay in the same data [8]. The LHCb 6 fb^{-1} Run 2 LHC data at 13 TeV, together with the improvements in the data selection for both runs, resulted in a nine-fold increase in the number of reconstructed $\Lambda_b^0 \rightarrow J/\psi p K^-$ decays (246,000 events) [10] and observation of new narrow $J/\psi p$ structures which were too faint to had been significant in the Run 1 data analysis. A second horizontal band is observed in the Dalitz plot (Fig. 83.1) near 4312 MeV in the $J/\psi p$ mass.

The 4450 MeV structure also appears to consist of two narrower peaks at 4440 and 4457 MeV. Performing a rigorous six-dimensional amplitude analysis of these faint $J/\psi p$ structures is challenging and has not been accomplished yet. Fortunately, the newly observed peaks are so narrow that it is not necessary to construct an amplitude model to prove that these states are not artifacts of interfering Λ^* resonances, as was previously demonstrated in Ref. [9]. Their masses and widths have been characterized by the LHCb (see Table 83.1) from one-dimensional fits to $J/\psi p$ mass distributions, with different levels of suppression of the Λ^* contributions, which peak at the lower $p K^-$ masses (Fig. 83.1). Such analysis is not sensitive to any broad $J/\psi p$ contributions. The histograms analyzed by the LHCb are available in tabular form at <https://www.hepdata.net/record/89271>.

The fit chosen by the LHCb for the central mass and width values is displayed in Fig. 83.2. The $P_{c\bar{c}}(4312)^+$ state (formerly known as $P_c(4312)^+$) peaks right below the $\Sigma_c^+ \bar{D}^0$ threshold and has statistical significance over 7.6σ . The $P_{c\bar{c}}(4457)^+$ state peaks right below the $\Sigma_c^+ \bar{D}^{*0}$ threshold, while the $P_{c\bar{c}}(4440)^+$ state peaks about 20 MeV below it. The significance of the two-peak versus one-peak hypothesis for the 4450 MeV structure is over 5.4σ , rendering the single peak interpretation of this region obsolete. The six-dimensional amplitude analysis reported in Ref. [8], which in addition to the structure near 4450 MeV, provided also evidence for the broad $P_{c\bar{c}}(4380)^+$ state, is obsolete since it used the single $P_{c\bar{c}}(4450)^+$ state and it lacked the $P_{c\bar{c}}(4312)^+$ state. Furthermore,

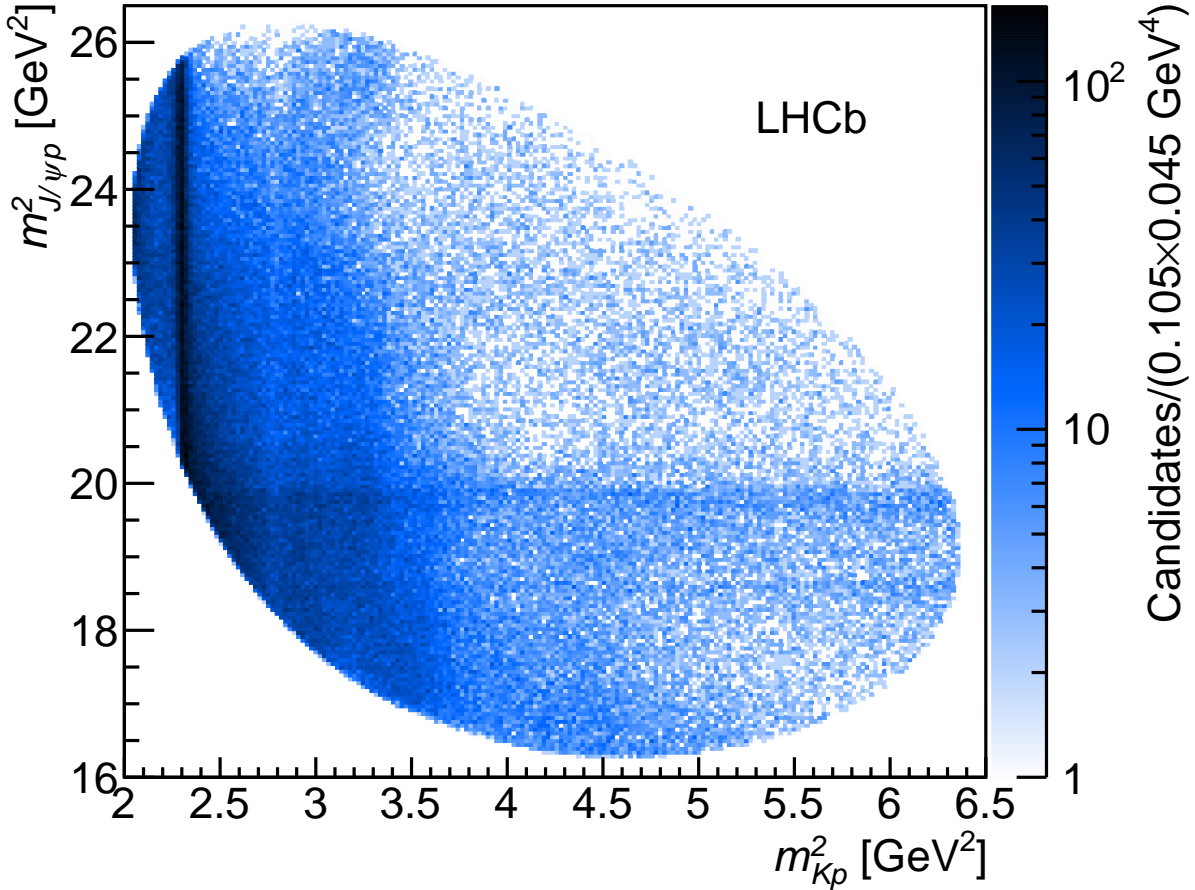


Figure 83.1: Dalitz plot distributions for $\Lambda_b^0 \rightarrow J/\psi p K^-$ decays as observed by LHCb.

it used the helicity formalism in which the half-integer spin of the proton was not aligned properly between the different Λ_b^0 decay chains [11, 12]. The newer one-dimensional analysis by LHCb [10] was not sensitive to wide $P_{c\bar{c}}^+$ states. The LHCb result from the six-dimensional amplitude analysis of the Cabibbo suppressed channel $\Lambda_b^0 \rightarrow J/\psi p \pi^-$ [13], which contains a statistically marginal evidence for the sum of the $P_{c\bar{c}}^+$ and the $T_{c\bar{c}1}^-$ (formerly known as $Z_c(4200)^-$) contributions, took extensive input from Ref. [8] and, like the $P_{c\bar{c}}(4380)^+$ state, should be treated with caution until the both amplitude analyses are completed on the enlarged data sets with the modified helicity formalism.

While $\Sigma_c \bar{D}^{(*)}$ states had been predicted [14–17] before the first LHCb results [8], after these results became known, many theoretical groups interpreted the $P_{c\bar{c}}(4450)^+$ and $P_{c\bar{c}}(4380)^+$ states in terms of diquarks and triquarks as building blocks of a compact pentaquark [18–24]. In a different strategy, a tentative attempt has been made to treat the full 5-body dynamics, leading to states below the lowest threshold for spontaneous dissociation [25]. In the first implementation of the former approach [18], the pentaquark mass splitting was generated mostly by the change of angular momentum between the sub-components (L) from zero to one, which would also make the heavier state narrower and of opposite parity. Explicit modeling of multiquark systems [26] questions if centrifugal barrier factor provides enough width suppression via spatial separation of c and \bar{c} quarks at these masses, as the phase space for $J/\psi p$ decay is very large (more than 400 MeV). Also, the observed mass splitting was too small to be only due to the mechanism proposed in Ref. [18] and required fine-tuning of such models. A variation of this model, in which the

Table 83.1: Summary of the narrow $P_{c\bar{c}}^+$ (formerly known as P_c^+) properties, interpreted as Breit-Wigner resonances. The central values are based on the fit displayed in Fig. 83.2.

State	M [MeV]	Γ [MeV] (95% CL)	\mathcal{R} [%]
$P_{c\bar{c}}(4312)^+$	$4311.9 \pm 0.7_{-0.6}^{+6.8}$	$9.8 \pm 2.7_{-4.5}^{+3.7} (< 27)$	$0.30 \pm 0.07_{-0.09}^{+0.34}$
$P_{c\bar{c}}(4440)^+$	$4440.3 \pm 1.3_{-4.7}^{+4.1}$	$20.6 \pm 4.9_{-10.1}^{+8.7} (< 49)$	$1.11 \pm 0.33_{-0.10}^{+0.22}$
$P_{c\bar{c}}(4457)^+$	$4457.3 \pm 0.6_{-1.7}^{+4.1}$	$6.4 \pm 2.0_{-1.9}^{+5.7} (< 20)$	$0.53 \pm 0.16_{-0.13}^{+0.15}$

heavy (cu) diquark couples with heavy \bar{c} to form colored triquark attracting the light diquark (ud), has been re-implemented for the narrow $P_{c\bar{c}}^+$ states [27]. In this model, the $P_{c\bar{c}}(4440)^+$ and $P_{c\bar{c}}(4457)^+$ states are accommodated via spin-orbit interactions for the $L = 1$ states, while the $P_{c\bar{c}}(4312)^+$ is one of the $L = 0$ states. However, the mass prediction for the latter is off by (-72 ± 29) MeV [27]. This work was later extended to $SU(3)_F$ [28]. The width dilemma becomes more severe in view of the narrow widths of the newly observed states (Table 83.1), especially for the $L = 0$ $P_{c\bar{c}}(4312)^+$ state, and requires a different origin of potential barrier between c and \bar{c} than angular momentum [27, 29], which remains a subject of theoretical controversy. Measurement of spin-parity of $P_{c\bar{c}}(4312)^+$, $P_{c\bar{c}}(4440)^+$ and $P_{c\bar{c}}(4457)^+$ will be crucial for testing these and alternative theoretical ideas discussed in the following.

More effective width suppression mechanism is offered by a loosely bound charmed baryon-anticharmed meson molecular model, in which c and \bar{c} can be separated by much larger distances, resulting in a smaller probability of them getting close enough to each other in order to make a J/ψ . Since molecular binding energy cannot be large, such molecules are in S -wave, so it has been realized early on that their masses must be near the sum of the baryon and meson masses and their spin and parity are inherited from their constituent hadrons, see e.g. discussion in [17]. The mass coincidence of the $P_{c\bar{c}}(4312)^+$ and of $P_{c\bar{c}}(4457)^+$ states, with the two related thresholds, $\Sigma_c^+ \bar{D}^0$ and $\Sigma_c^+ \bar{D}^{*0}$, provides very strong experimental evidence in favor of this interpretation. Given how close $P_{c\bar{c}}(4312)^+$ is to the $\Sigma_c^+ \bar{D}^0$ threshold, it might be a virtual rather than a bound state [30]. Since the spins of Σ_c^+ and of \bar{D}^{*0} can be combined in two different ways, the narrow $P_{c\bar{c}}(4440)^+$ peak also finds natural explanation in this physical picture. It cannot be a virtual state since it is sufficiently below the $\Sigma_c^+ \bar{D}^{*0}$ threshold.

It is worth stressing that other baryon-meson combinations, $\Lambda_c^{(*)+} \bar{D}^{(*)0}$ and $\chi_{cJ} p$ are not expected to bind [14, 31]. Before the first pentaquark observation [8] heavy quark symmetry was used to show that, in addition to the three $\Sigma_c \bar{D}^{(*)0}$ states, one expects four $\Sigma_c^* \bar{D}^{(*)0}$ states, for a total of seven [32]. Indeed, additional states at, or below, the $\Sigma_c^{*+} \bar{D}$ and $\Sigma_c^{*+} \bar{D}^*$ thresholds, are expected [33–36]. Since Σ_c^{*+} width is likely around 15 MeV [37], more than the width of either $P_{c\bar{c}}(4312)^+$ or $P_{c\bar{c}}(4457)^+$, it is important to keep in mind that a molecule is typically as broad as the constituents¹ [38–40]. There is no significant evidence for $\Sigma_c^* \bar{D}^{(*)}$ states in the present LHCb data set [10, 41]. Larger data sets are expected from the Upgraded LHCb experiment. For a review on hadronic molecules, and a recent survey in a particular approach, see respectively Refs. [42, 43].

It is useful to consider the $P_{c\bar{c}}(4312)^+$, $P_{c\bar{c}}(4440)^+$ and $P_{c\bar{c}}(4457)^+$ narrow pentaquarks together with several analogous exotic states with hidden charm and bottom in the meson sector. This provides additional significant motivation for the molecular model. At least five exotic mesons are close to thresholds of two heavy-light mesons: $\chi_{c1}(3872)$ (formerly known as $X(3872)$) [44–47], $T_{b\bar{b}1}(10610)$ and $T_{b\bar{b}1}(10650)$ (formerly $Z_b(10610)$ and $Z_b(10650)$) in the bottomonium sector [48–

¹This feature gets changed if systems are more deeply bound.

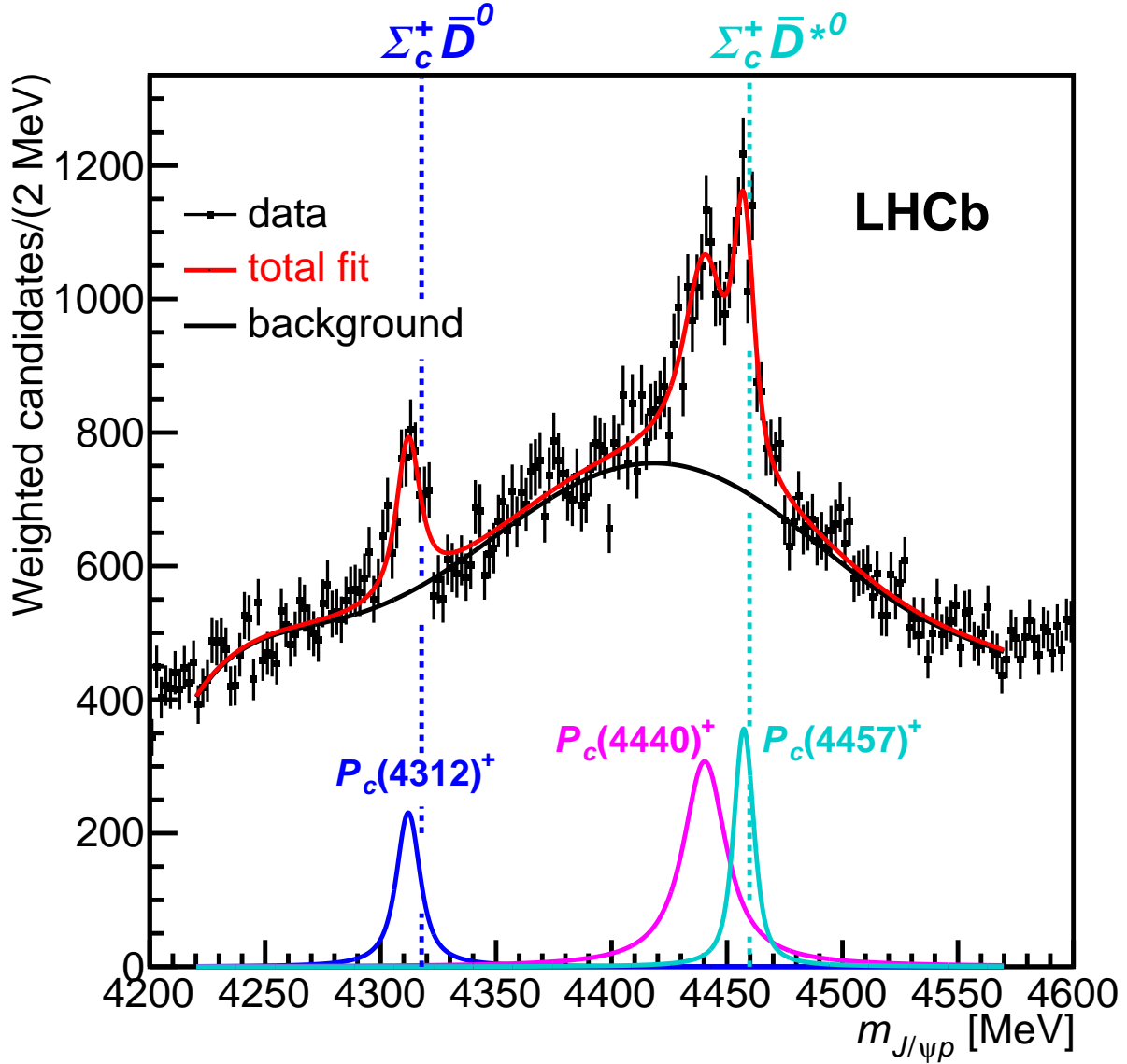


Figure 83.2: Fit to the $J/\psi p$ mass distribution, in which events were weighted to suppress $\Lambda^* \rightarrow pK^-$ backgrounds, of three Breit-Wigner functions and a sixth-order polynomial background. This fit was used to determine the central values of the masses and widths of the P_{cc}^+ states (formerly known as P_c^+) reported by LHCb. The mass thresholds for the $\Sigma_c^+ \bar{D}^0$ and $\Sigma_c^+ \bar{D}^{*0}$ final states are superimposed.

52] and $T_{c\bar{c}1}(3900)$ (formerly $Z_c(3900)$) [53–57] and $T_{c\bar{c}1}(4020)$ (formerly $Z_c(4020)$) [58–60] in the charmonium sector (see Table II in Ref. [61]; for reviews of experimental information see Ref. [62,63], as well as *Spectroscopy of Mesons Containing Two Heavy Quarks* and *Heavy Non- $q\bar{q}$ Mesons* in the current Review of Particle Properties. These states share several important features: a) their masses are near thresholds and their spin and parity correspond to S -wave combination of the two mesons; b) they are very narrow, despite very large phase space for decay into quarkonium + pion(s); c) the branching fractions for “fall apart” mode into two mesons are much larger than branching fractions for decay into quarkonium and pion(s). So far, there is no experimental evidence for states at two pseudoscalar thresholds ($D\bar{D}$ and $B\bar{B}$), suggesting that pseudoscalar exchange is essential for

binding in meson-meson systems.

The above provide a strong hint that these states are deuteron-like loosely bound states of two heavy mesons [64–72]. It is then natural to conjecture that similar bound states might exist of two heavy baryons [73, 74], or a meson and a baryon or a baryon and an antibaryon, leading to a rather accurate prediction of the $P_{c\bar{c}}(4457)^+$ mass as $3/2^- \Sigma_c \bar{D}^*$ molecule (the mass threshold is 4460 MeV for $\Sigma_c^+ \bar{D}^{*0}$ and 4464 MeV for $\Sigma_c^{++} D^{*-}$) [17, 61], following similar predictions obtained in a wider framework of doubly heavy baryon-meson hadronic molecules, which might include mixtures of various two-hadron states [14–16, 31]. However, single pion exchange is not possible in $\Sigma_c^+ \bar{D}^0$ system. Thus the existence of $P_{c\bar{c}}(4312)^+$ suggests a more general binding mechanism in baryon-meson molecules, e.g. vector or two-pion exchanges, and/or coupled-channel interactions. Two-pion exchange in $D\bar{D}$ system is highly suppressed, because the intermediate state is $D^* \bar{D}^*$, which is 282 MeV heavier than $D\bar{D}$. On the other hand, in the $\Sigma_c \bar{D}$ system the intermediate $\Lambda_c^+ \bar{D}^*$ state is only 25 MeV lighter than $\Sigma_c \bar{D}$, and therefore does not have to suffer significant suppression, providing a possible binding mechanism [75]. In a generic hadronic molecule it is essential that the two hadrons are heavy, in order to minimize the repulsive kinetic energy [73, 74, 76].

Following the initial LHCb discovery [8], several groups carried out a detailed analysis of the $P_{c\bar{c}}^+$ states as hadronic molecules [77–86] followed by further analyses [35, 87–111] after the updated LHCb results [10]. Partial widths of all the allowed decay channels for the $P_{c\bar{c}}$ states have been estimated within a specific model in the molecular picture [112]. The most striking suggestion is that $P_{c\bar{c}}(4312)^+$ decays are totally dominated by the $\Lambda_c^+ \bar{D}^{*0}$ channel. This channel is also suggested to be very prominent in decays of $P_{c\bar{c}}(4440)^+$ and $P_{c\bar{c}}(4457)^+$. But other scenarios are possible, as shown by a recent theoretical analysis, allowing for the most general scattering potential of the baryon-meson system consistent with QCD symmetries at leading order in a momentum counting [113]. They found that both large and vanishing transitions to $\Lambda_c^+ \bar{D}^{(*)0}$ channels are allowed. Clearly, experimental determination of the branching fraction of these channels is of high priority.

The $P_{c\bar{c}}$ states have also been interpreted as so called hadro-charmonium [114], a bound state of relatively compact charmonium states with light hadronic matter. It was proposed that $P_{c\bar{c}}(4440)^+$ and $P_{c\bar{c}}(4457)^+$ are spin-split $\psi(2S)p$ bound states with $J^P = \frac{1}{2}^-$ and $\frac{3}{2}^-$, while $P_{c\bar{c}}(4312)^+$ is a $\chi_{c0}p$ bound state with $J^P = \frac{1}{2}^+$ [115]. While very interesting from the theoretical point of view, it is not at all clear why the binding energies between charmonia and the nucleon should conspire to produce states so close to the $\Sigma_c \bar{D}$ and $\Sigma_c \bar{D}^*$ thresholds. Moreover, the predicted widths of $P_{c\bar{c}}(4440)^+$ and $P_{c\bar{c}}(4457)^+$ are too big by a factor ~ 2 -3. One should also keep in mind that the molecular and hadro-charmonium pictures provide opposite predictions for the parity of $P_{c\bar{c}}(4312)^+$. In principle LHCb can check the spin and parity through partial wave analysis, but at present it is not known if systematic uncertainties can be sufficiently reduced to make such an analysis conclusive.

Shortly after the initial experimental discovery it was conjectured that the $P_{c\bar{c}}(4450)^+$ reflects the presence of a triangle singularity near the $\chi_{c1}p$ threshold [116–119]. These explanations are no longer viable, since the $P_{c\bar{c}}(4440)^+$ mass is not at any threshold and the $P_{c\bar{c}}(4312)^+$ and $P_{c\bar{c}}(4457)^+$ peak slightly below the $\Sigma_c^+ \bar{D}^0$ and $\Sigma_c^+ \bar{D}^{*0}$ thresholds. The $P_{c\bar{c}}(4457)^+$ mass is exactly at $\Lambda_c^+ \bar{D}^0$ threshold, but LHCb has demonstrated that the observed peaking is narrower in the data than expected from the triangle-diagram when a realistic width of the excited D_s^- state exchanged in the triangle is used (Supplemental Material in Ref. [10]).

More extensive pre-2019 reviews of some of the theoretical issues can be found in Refs. [120, 121]. Two recent relevant reviews are Refs. [122, 123].

So far the $P_{c\bar{c}}^+$ states have been observed by only one experiment in only one channel. It is essential to explore other possible experimental channels, such as $P_{c\bar{c}}^+ \rightarrow \Lambda_c^+ \bar{D}^{(*)0}$, $\eta_c p$ [113]. These channels are however much more experimentally challenging than $P_{c\bar{c}}^+ \rightarrow J/\psi p$. The decays

$\Lambda_b^0 \rightarrow \eta_c p K^-$ [124], $\Lambda_b^0 \rightarrow \Lambda_c^+ \bar{D}^{(*)0} K^-$ [125] and $\Lambda_b^0 \rightarrow \Sigma_c^{(*)++} \bar{D}^{(*)-} K^-$ [126] have been observed by the LHCb, but larger data samples are needed to probe for P_{cc}^+ signals. So far, search for prompt pp production of pentaquarks by the LHCb in charm hadron final states, including $\Lambda_c^+ \bar{D}^0$ and $\Lambda_c^+ \pi^+ \bar{D}^-$, resulted in upper limits only [127]. Search for $P_{cc}^+ \rightarrow p J/\psi$ states in inclusive decays of $\Upsilon(1S)$ and $\Upsilon(2S)$ produced in e^+e^- annihilation by the Belle experiment also resulted in upper limits [128].

Proposals have also been made to search for heavy pentaquarks in photo-production [129–136]. Ref. [137] discusses photoproduction within the string-junction physical picture of the pentaquarks. Photoproduction is also related to recent work on $J/\psi(\eta_c)N$ scattering on the lattice [138] and on computation of $J/\psi(\eta_c)N$ and $\Upsilon(\eta_b)N$ cross sections [139]. In addition, pentaquark production has been discussed in the context of antiproton-deuterium collisions [140], of heavy ion collisions at LHC [141], in pA collisions [142] and in pion-induced processes [143–145]. The GlueX Collaboration reported negative search results for the P_{cc}^+ states in photo-production at JLAB [146, 147], $\gamma p \rightarrow (J/\psi \rightarrow e^+e^-)p$. Within the large experimental errors and considerable theoretical model dependence these results do not contradict the molecular interpretations of the narrow P_{cc}^+ states. In particular, vector-meson dominance often assumed in theoretical modelling may not hold for near-threshold J/ψ production, and $\Lambda_c \bar{D}^{(*)0}$ intermediate states may significantly contribute to the $J/\psi p$ production complicating probing for the P_{cc}^+ states [148, 149].

As noted in e.g. [17], bottom analogues of the P_{cc}^+ might well exist, but experimental search for such states involves very significant challenges. It is therefore hardly surprising that they have not been observed so far. A detailed discussion is beyond the scope of the current review.

The LHCb collaboration obtained a 3.1σ evidence for a $P_{cc}^+ \rightarrow J/\psi p$ state in the four-dimensional amplitude analysis of about 800 $B_s^0 \rightarrow J/\psi p \bar{p}$ ($J/\psi \rightarrow \mu^+ \mu^-$) decays [150]. The mass of the state, $4337_{-4}^{+7} \pm 2$ MeV, is not compatible with the the $P_{cc}(4312)^+$ state at 3.1 standard deviations. The width is relatively small, $29_{-12}^{+26} \pm 14$ MeV. The present data do not provide sufficient discrimination between various J^P assignments. Its mass is about 19 MeV higher than the $\Sigma_c^+ \bar{D}^0$ threshold and about 16 MeV lower than the $\chi_{c0} p$ threshold. At present, no specific explanation for this structure has been proposed, but some intriguing ideas have been raised in Ref. [151]. Since the statistical significance of this evidence is marginal, more data are required before this state is considered experimentally established.

Similarly inconclusive 3.1σ evidence for a $P_{ccs}^0 \rightarrow J/\psi \Lambda$ structure was observed by the LHCb collaboration in the six-dimensional amplitude analysis of about 1750 $\Xi_b^- \rightarrow J/\psi \Lambda K^-$ ($J/\psi \rightarrow \mu^+ \mu^-$, $\Lambda \rightarrow p \pi^-$) decays [12]. The strange counterparts of P_{cc}^+ states have been predicted in both molecular and compact pentaquark models [15, 99, 101, 152–154]. When interpreted as a single peak, its mass, $4458.8 \pm 2.9_{-1.1}^{+4.7}$ MeV, is 15 MeV above the $\Xi_c^{\prime 0} \bar{D}^0$ threshold and 18 MeV below the $\Xi_c^0 \bar{D}^{*0}$ threshold. Its width, $17.3 \pm 6.5_{-5.7}^{+8.0}$ MeV, is relatively narrow, thus plausibly could be interpreted as a loosely bound $\Xi_c^0 \bar{D}^{*0}$ state. However, in the latter model two states are expected with J^P equal to $1/2^-$ and $3/2^-$. In fact, the LHCb data are consistent with such hypothesis, under which 4454.9 ± 2.7 MeV ($\Gamma = 7.5 \pm 9.7$ MeV) and 4467.8 ± 3.7 MeV ($\Gamma = 5.2 \pm 5.3$ MeV) mass (width) estimates are obtained (statistical errors only). It is worth noting, that the $SU(3)$ flavor structure of $\Xi_c^0 \bar{D}^{*0}$ states is different from that of $\Sigma_c^+ \bar{D}^{*0}$ states, since Ξ_c^0 belongs to the charmed baryon triplet, together with Ξ_c^+ and Λ_c^+ , where the two light quarks form a spin-zero diquark, unlike Σ_c^+ , which together with $\Xi_c^{\prime 0}$ and Ω_c^0 belongs to the charmed baryon sextet, where the two light quarks form a spin-1 diquark. More data are required to experimentally establish this structure, clarify its composition, and determine the related quantum numbers.

If the two states at 4455 MeV and 4468 MeV indeed correspond to a $\Xi_c^0 \bar{D}^{*0}$ molecule, there perhaps exist two other states, corresponding to $\Xi_c^{\prime} \bar{D}^*$ [15, 99, 101, 152–154], with a mass shifted

upwards by approximately $\Xi'_c - \Xi_c$ mass difference [155, 156], i.e. about 108 MeV [37].

More recently, the LHCb experiment observed highly significant ($> 14\sigma$) pentaquark state $P_{c\bar{c}s}(4338)^0 \rightarrow J/\psi \Lambda$ (formerly known as $P_{cs}(4338)$) in the six-dimensional amplitude analysis of $4620 \pm 70 B^- \rightarrow J/\psi \Lambda \bar{p}$ decays [157]. Its mass $4338.2 \pm 0.7 \pm 0.4$ MeV is right at the $\Xi_c \bar{D}$ threshold (Fig. 83.3), its width is narrow $7.0 \pm 1.2 \pm 1.3$ MeV, and its spin is 1/2, with a preference for negative parity, which all fits the molecular model very well. This makes the $P_{c\bar{c}s}(4338)^0$ state a likely $\Xi_c^0 \bar{D}^0$ analog of the $P_{c\bar{c}}(4312)^+$ state in $\Sigma_c^0 \bar{D}^0$ system. In addition, as in the $P_{c\bar{c}s}(4459)^0$ case, a $\Xi'_c \bar{D}$ state is expected, for a total of three additional strange pentaquarks [156]. Experimental determination whether yet additional $\Xi_c^{(*,')} \bar{D}^{(*)0}$ states actually exist will provide a useful testing ground for the various theoretical approaches which have been used to predict them.

Search for the $P_{c\bar{c}s}^0$ states in decays to $\Lambda_c^+ D_s^-$ have been recently performed by the LHCb using a

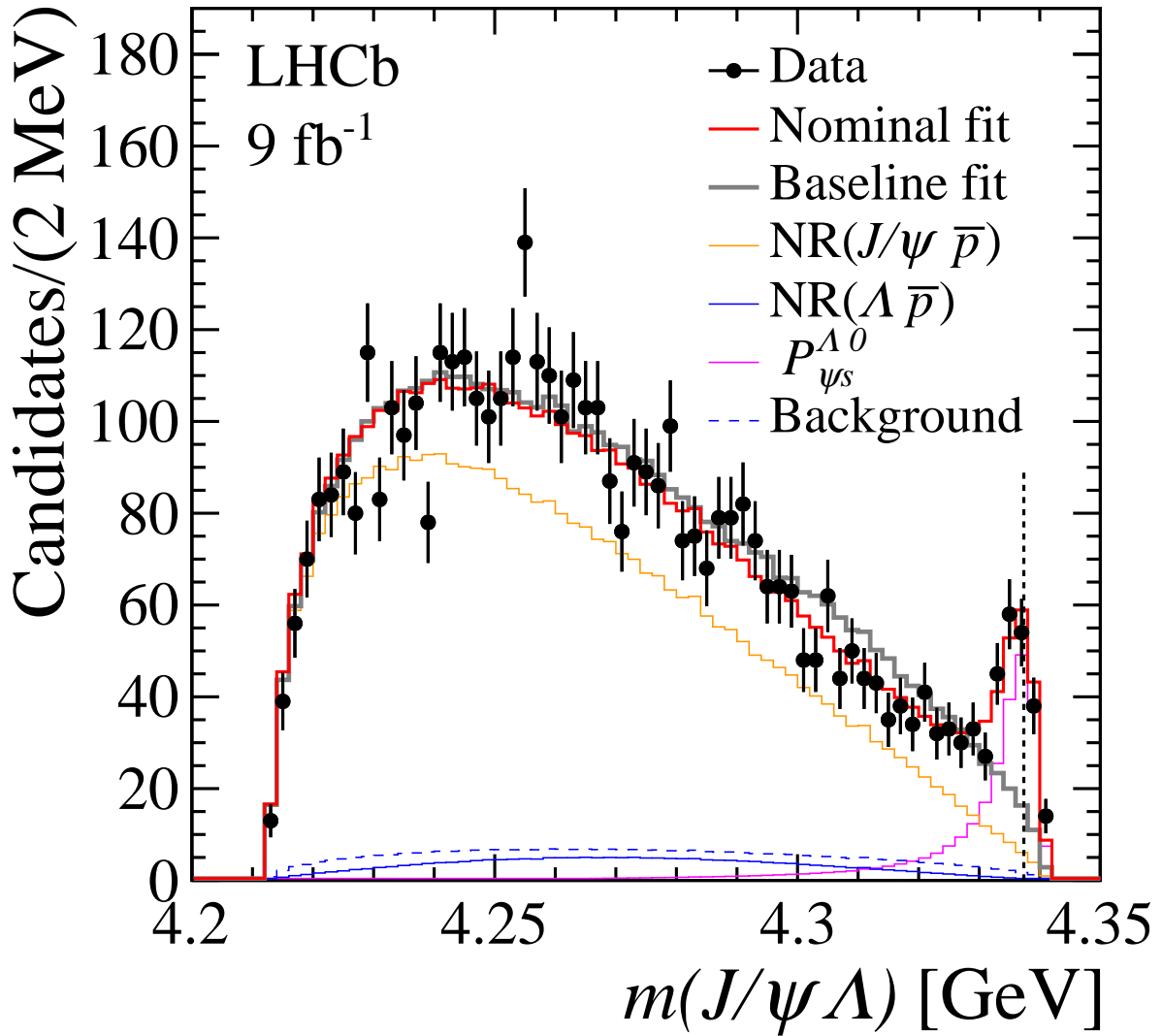


Figure 83.3: Distribution of invariant $J/\psi \Lambda$ mass, with the projection of the amplitude fit model superimposed. The model without the $P_{c\bar{c}s}(4338)^0$ state (labeled as $P_{\psi s}^{\Lambda 0}$) is also shown in grey. The $\Xi_c^+ D^-$ baryon-meson threshold is indicated with a vertical dashed line.

small sample of $\Lambda_b^0 \rightarrow \Lambda_c^+ D_s^- K^+ K^-$ decays [158]. Search by the Belle experiment for $P_{c\bar{c}s}^+ \rightarrow J/\psi \Lambda$ states in inclusive decays of $\Upsilon(1S)$ and $\Upsilon(2S)$, produced in e^+e^- annihilation, yielded a hint of the $P_{c\bar{c}s}(4459)^0$ state and upper limits on production of the $P_{c\bar{c}s}(4338)^0$ state [159]. When combining the $\Upsilon(1S)$ and $\Upsilon(2S)$ samples together, a peak in $J/\psi \Lambda$ mass is observed at $4471.7 \pm 4.8 \pm 0.6$ MeV with a width of $22 \pm 13 \pm 3$ MeV, which are consistent with the LHCb results at 1.8σ and 0.3σ level, respectively. A local statistical significance of this peak is 3.8σ (not including systematic effects), which is an appropriate figure of merit if the mass and width are considered to be consistent between the LHCb and Belle results. A global signal significance, appropriate measure for stand-alone unbiased search, is 2.8σ (no systematic effects folded in). Imposing Gaussian constraints on the mass and width to the LHCb results, the $P_{c\bar{c}s}(4459)^0$ peak fitted to the Belle data is 3.3σ significant including systematic uncertainties. This result may be affected by the single-peak interpretation of the LHCb data, which has not been established as discussed above. More $\Upsilon(1S)$ and $\Upsilon(2S)$ data are highly desired to verify existence of this mass structure.

In hidden-charm exotics discussed above, the charmed and the anticharmed quarks can form a charmonium and thereby decouple from the light quarks. The molecular model provides an efficient mechanism to suppress such decays, thus making these states narrow. Compact direct color couplings between quarks, in diquark approach, are missing an obvious width suppression mechanism, thus could lead to broader states. In fact, there is plenty of evidence for them in form of broader tetraquark mass structures in $J/\psi \phi$ [160–166], $J/\psi J/\psi$ [167–169], $T_{c\bar{c}1}(4430)^+ \rightarrow \psi(2S)\pi^+$ (formerly $Z_c(4430)^+$) [170–172] and others, although alternative explanations of these structures have been also proposed. Analogous configurations may also exist for pentaquarks, but there is no firm evidence for them yet.

A relatively new theoretical approach to hidden-charm exotics is based on the recognition that heavy quarks move slowly compared to their light quark partners. This is analogous to atomic molecules, which have been successfully described as heavy nuclei vibrating slowly in Born-Oppenheimer (BO) potential, generated by fast-moving electrons. Unlike the hadro-charmonium picture, in which $c\bar{c}$ pair is assumed to be in a polarized color-singlet state, the BO approach assumes that the $c\bar{c}$ pair is in color-octet state [173–176]. Perturbative QCD predicts repulsive $1/r$ potential at short $c\bar{c}$ distances, while LQCD predicts a confining linear potential at large $c\bar{c}$ distances. The transition from octet to singlet charmonium requires hard gluon interaction. This suppresses decays to a charmonium and a light baryon, making the states narrow. To avoid the unobserved rich spectrum of bound states expected in the confining potential, it has been proposed that the potential transitions smoothly to a constant term at large distances, due to light quarks attaching themselves to the heavy quarks as they separate from each other, creating heavy-light charmed baryon – anticharmed meson pair. Thus, the hadronic molecule physical picture naturally emerges as the long-distance limit of the QCD-motivated BO approach. The baryon-meson threshold can be approached from below, creating a shallow potential well with few bound state(s) just below the threshold (e.g. $\Sigma_c^{(*)}\bar{D}^{(*)}$ case); smoothly from above, creating no bound states ($\Lambda_c\bar{D}^{(*)}$ case); or the intermediate potential raising to the confining part can overshoot the threshold somewhat, generating a bound state slightly above the threshold. This mechanism can accommodate the narrow tetraquark states observed just above the $D^*\bar{D}^{(*)}$ and $B^*\bar{B}^{(*)}$ thresholds. The non-relativistic Schrödinger equation can be used to solve the BO potential for bound state energies. The hyperfine structure is created by coupling the total angular momentum of the light quark (diquark) to heavy quark (antiquark) spins. If all combinations of the angular momenta of light quarks are allowed, the number of states and their spin-parity match the predictions of the molecular model [175]. However, in the BO approach the constituents are colored heavy quarks, rather than color-neutral heavy hadrons, providing for a different modelling approach and better prospects for a direct input

from QCD via simulations of BO potentials on the lattice. Unlike in the naive molecular model, the short-range structure of the bound states is predictable. The BO approach predicts fewer states, with a different spin-parity pattern if not all values of total the angular momenta of light quarks are assumed to create bound states [176].

The hidden-charm exotic states, should not be confused with exotic hadrons containing two heavy quarks, rather than a heavy quark and a heavy antiquark. Decoupling from the light quarks is impossible in exotics which contain two heavy quarks. This has far-reaching consequences. The first tetraquark of the latter type, i.e. containing two heavy quarks, has been reported by LHCb [177, 178]. A comprehensive discussion of tetraquark candidates can be found in the “Heavy non- QQ Mesons” review.

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